

A New Controller for LC-Hybrid Active Power Filter for Power Quality Improvement

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ABSTRACT:

A deadbeat current controller for an LC coupling hybrid active power filter (LC-HAPF) is suggested in this thesis, and it can track with the reference compensation current with low steady-state error and quick dynamic response. Furthermore, it allows the LC-HAPF to operate at a set switching frequency with minimal output current ripples, lowering the filtering circuit's footprint. First, the single-phase equivalent circuit is used to derive the mathematical model of the deadbeat current controller for the LC-HAPF. The closed-loop control block diagram, as well as its s-domain model, is then suggested and constructed. The suggested deadbeat current controller's stability problem and parameter design are then evaluated and explained. Finally, simulation results of the deadbeat current controller are analyzed for the LC-HAPF to the conventional hysteresis band pulse-width modulation (PWM) control, the proportional-integral (PI) control, and the proportional multi-resonant (PMR) control, demonstrating its effectiveness and superior compensating performances.

I. INTRODUCTION

The Circuit Configuration of LC-HAPF Fig.1 illustrates the system configuration of a three-phase four-wire center-split LC-HAPF, where the subscript 'x' denotes phase a, b, c, n. v_{sx} is the system voltage, v_x is the load voltage, L_s is the system inductance which can be neglected because of its small value. i_{sx} , i_{cx} and i_{Lx} are the system, inverter, load current for each phase respectively. L_{cx} and C_{cx} are the coupling inductor and capacitor of the HAPF. C_{dc} , V_{dcU} and V_{dcL} are

the DC capacitor, upper and lower DC capacitor voltages with $V_{dcU} = V_{dcL} = 0.5V_{dc}$. The midpoint of DC-link is assumed as ground reference point g.

So that the voltage source inverter (VSI) line-to-ground voltage v_{invx-g} equals to VSI line-to-neutral voltage v_{invx-n} . T_{1x} and T_{2x} stand for the trigger signal of the switching device. The loads are inductive nonlinear load which are composed of three single-phase diode bridge rectifiers. It can be considered as harmonics producing loads. Fig. 5.2 shows the LC-HAPF single-phase equivalent circuit, where v_{Cx} and v_{Lx} represent the capacitor and inductor voltages. Parameters Design of Passive Part of LC-HAPF The coupling L_{cx} and C_{cx} of the LC-HAPF are designed based on harmonic current of loading and the average fundamental reactive power consumption.

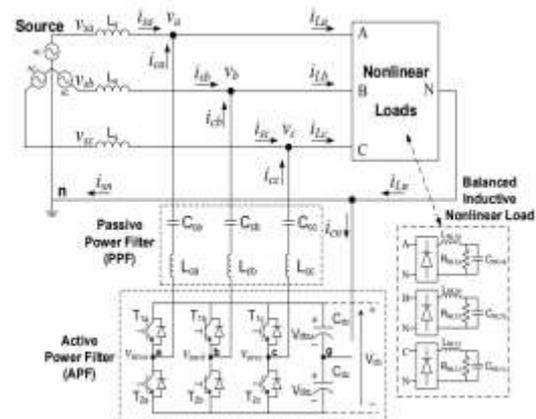


Fig. 1 System configuration of a three-phase four-wire center-split LCHAPF.

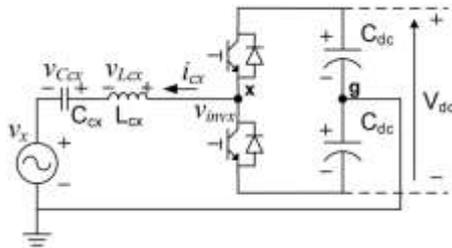


Fig. 2. LC-HAPF single-phase equivalent circuit.

Generally, the dominant harmonic orders in three-phase four-wire system are odd orders ($n = 3, 5, 7, \dots$) and each LC branch can filter one single harmonic order. More LC branches can be added to the LC-HAPF to filter more harmonic current orders. Otherwise, the minimum DC-link voltage should be increased as discussed in [32]-[34]. The design criteria of the L_{cx} and C_{cx} is described in the following. The relationship between the load fundamental reactive power and reactance of L_{cx} and C_{cx} can be expressed in (1), where ω is the fundamental angular frequency, V_x represents the root-mean-square load voltage, Q_{Lxf} is the load reactive power under fundamental frequency, X_{Ccx} is reactance of coupling capacitor and X_{Lcx} is reactance of coupling inductor. After that, it can solve the values of X_{Ccx} and X_{Lcx} with the help of (2). Note that n is the order of filtering harmonic frequency. In this paper, the dominant harmonic current order of the full bridge diode rectifier loading are 3rd and 5th orders, respectively. To reduce the cost and size of their coupling LC, they are tuned at the 5th order ($n = 5$) harmonic frequency.

II. DEADBEAT CURRENT CONTROLLER OF LC-HAPF

Proposed Deadbeat Current Controller of LC-HAPF The conventional hysteresis current PWM control for the LC-HAPF will cause significant steady-state error and also the switching frequency is variable, which implies complexity in design of the filtering circuits and the stable feedback controller for wide range operation. Thus, hysteresis PWM control usually generates large ripple and deteriorates the current harmonics compensation performance of the LC-HAPF. To overcome these problems, a deadbeat current controller will be proposed in this section. Fig. 3, shows a control block diagram of the proposed deadbeat current controller while Fig. 4 represents its s-domain model, in which the further analysis and discussion of the design of the controller will be presented in the following.

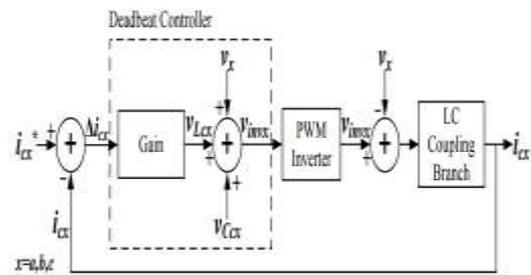


Fig. 3. Control block diagram of deadbeat current controller.

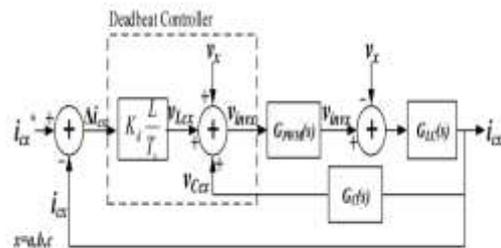


Fig. 4. s-domain model of deadbeat current controller.

Fig. 5 also shows its waveforms of generating

PWM trigger signals. The key concept of this controller is to find out the duty ratio d_o of the switching devices in every switching period which is fixed in every single period ($T_{SW} = 1/f_{SW}$) based on the LC-HAPF system parameters, sampling period T_s and sensed instantaneous load voltage, compensation current and coupling capacitor voltage signals. After that, the trigger PWM signals for the switching devices can be generated by comparing the computed d_o with a triangular wave carrier with a fixed switching frequency f_{SW} .

In addition, this deadbeat current control strategy can achieve fixed switching frequency, reduce the steady-state error, improve the performance of reference compensating current tracking and compensation performance for the LC-HAPF, which will be verified in the below section.

In the following, the mathematical modelling for the deadbeat current controller for the LC-HAPF will be introduced and discussed.

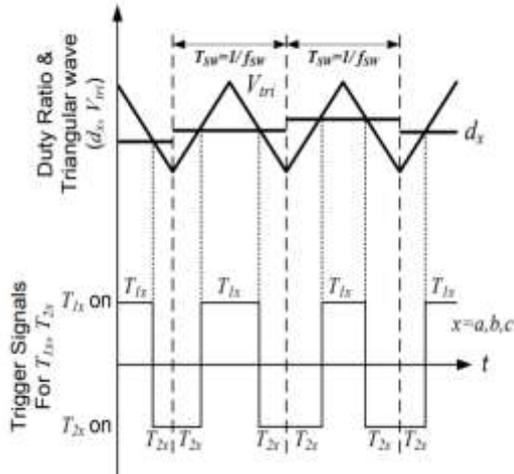


Fig. 5. Waveforms of generating PWM trigger signals with deadbeat current control.

III. MATHEMATICAL MODELLING

The reference compensating current i_{cx}^* can be obtained by using the instantaneous p-q theory [46]. From Fig. 2, the characteristic equation of the LC-HAPF system can be expressed as:

$$v_{L_{cx}}(t) = L_{cx} \frac{di_{cx}(t)}{dt} = v_{imx}(t) - v_x(t) - v_{C_{cx}}(t) \quad (1)$$

Reforming (5.1), the averaged model of the LC-HAPF in the stationary coordinate system can be represented as:

$$v_{imx}(t) = d_x(t) \cdot v_{dc} = L_{cx} \frac{di_{cx}(t)}{dt} + v_x(t) + v_{C_{cx}}(t) \quad (2)$$

Where d_x refers to the duty ratio in one phase of the VSI in each small-time interval. It can be separated by upper and lower switch part as follows:

$$d_{1x}(t) + d_{2x}(t) = 1 \quad (3)$$

The summation of them is equal to 1 since the switching ON and OFF time of the upper and lower switches of the VSI is equal to one control switching period ($T_{sw}=1/f_{sw}$). From (3), the characteristic equation (1) becomes:

$$[d_{1x}(t) - d_{2x}(t)] \cdot v_{dc} = L_{cx} \frac{di_{cx}(t)}{dt} + v_x(t) + v_{C_{cx}}(t) \quad (4)$$

For digital implementation of the PWM control algorithm and the consideration about the filter inductance deviation, the instantaneous averaged model in (4) can be represented in discrete time with a step size of k as in (5):

$$[d_{1x}(k) - d_{2x}(k)] \cdot v_{dc} = K_d L_{cx} \frac{i_{cx}(k+1) - i_{cx}(k)}{T_s} + v_x(k) + v_{C_{cx}}(k) \quad (5)$$

Where K_d is inductance deviation coefficient that can be treated as control variable, T_s is the sampling period. $i_{cx}(k+1)$ represents the reference compensating current i_{cx}^* . Hence, combining (3) and (5), the duty ratio of one phase VSI is now obtained as:

$$d_{1x}(k) = \frac{1}{2} \left[1 + \frac{K_d L_{cx} \frac{i_{cx}(k) - i_{cx}(k)}{T_s} + v_x(k) + v_{C_{cx}}(k)}{v_{dc}} \right]$$

$$d_{2x}(k) = \frac{1}{2} \left[1 - \frac{K_d L_{cx} \frac{i_{cx}(k) - i_{cx}(k)}{T_s} + v_x(k) + v_{C_{cx}}(k)}{v_{dc}} \right] \quad (5.6)$$

Usually, find out the duty ratio of either upper or lower switch ($d_{Ux}(k)$ or $d_{Lx}(k)$) is enough, then find out the duty ratio of the remaining switch by using (3). After that, the duty ratio is used to compare with the fixed frequency triangular carrier wave in order to generate PWM signal for the switching devices in VSI. The switching frequency of the VSI is the same as the frequency of the triangular carrier wave. Stability and Parameter Design of Deadbeat Current Controller According to (7) and Fig.3, Fig.4 shows the s-domain closed-loop control block diagram model for the deadbeat current controller of the LC-HAPF. The information of each block will be given in below. GPWM(s) is an average s-domain model, note that the PWM VSI can be assumed as unity gain [44], in which Fig.6 shows the details of GPWM(s). To accurately describe the GPWM(s), computation delay, sampler and zero order hold (ZOH) as in s-domain should be considered. The transfer function of the PWM VSI can be expressed as:

$$G_{PWM}(s) = \frac{e^{-T_s s} (1 - e^{-T_s s})}{T_s \cdot s} \quad (7)$$

Where T_s is the sampling time. For obtaining a rational transfer function, delays are usually approximated by poles and then, Pade' approximation (8) can be applied to (7).

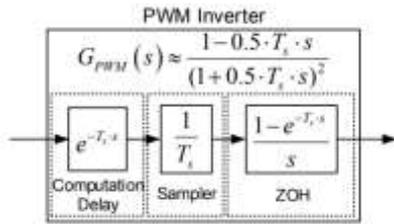


Fig. 5.6. s-domain model of PWM inverter zeros.

$$e^{-T_s s} \approx \frac{1 - 0.5 \cdot T_s \cdot s}{1 + 0.5 \cdot T_s \cdot s} \quad (8)$$

Substitute (8) into (7) yields:

$$G_{PWM}(s) = \frac{e^{-T_s s} (1 - e^{-T_s s})}{T_s \cdot s} \approx \frac{1 - 0.5 \cdot T_s \cdot s}{(1 + 0.5 \cdot T_s \cdot s)^2} \quad (9)$$

Where $G_{LC}(s)$ and $G_C(s)$ are the LC coupling branch and coupling capacitor impedance in s-domain, which can be expressed as follows:

$$G_{LC}(s) = \frac{C_\alpha s}{L_\alpha C_\alpha s^2 + 1}$$

$$G_C(s) = \frac{1}{C_\alpha s} \quad (10)$$

The transfer function according to Fig. 4 can be deduced as:

$$i_{\alpha}(s) = G_{CL_i}(s) \cdot i_{\alpha}^*(s) + G_{CL_v}(s) \cdot v_s(s)$$

$$= \frac{K_d \frac{L}{T_s} G_{PWM}(s) G_{LC}(s)}{1 + K_d \frac{L}{T_s} G_{PWM}(s) G_{LC}(s) - G_{PWM}(s) G_{LC}(s) G_C(s)} i_{\alpha}^*(s)$$

$$+ \frac{G_{LC}(s) (G_{PWM}(s) - 1)}{1 + K_d \frac{L}{T_s} G_{PWM}(s) G_{LC}(s) - G_{PWM}(s) G_{LC}(s) G_C(s)} v_s(s) \quad (11)$$

Where $G_{CL_i}(s)$ is the system closed-loop transfer function between i_{α} and i_{α}^* , $G_{CL_v}(s)$ is the system closed-loop transfer function between i_{α} and v_s . To analyse the stability of the proposed deadbeat current controller, the range of the control coefficient K_d must be found. Theoretically, K_d should be as high as possible to obtain high gain, fast response and low steady-state error at low-order harmonics frequency and fundamental frequency.

However, system stability is under the 1st priority consideration. The stability margin would be sacrificed with high K_d gain. Therefore, with the help of the Routh's stability criterion and Fig. 4, the analysis of the range of K_d is based on the characteristic equation ($q(s) = 0$) of the closed-loop

transfer function between i_{α} and i_{α}^* . The closed-loop transfer function between i_{α} and i_{α}^* is shown in (12) and its characteristic equation can be expressed in (13).

$$G_{CL_i}(s) = \frac{K_d \frac{L}{T_s} G_{PWM}(s) G_{LC}(s)}{1 + K_d \frac{L}{T_s} G_{PWM}(s) G_{LC}(s) - G_{PWM}(s) G_{LC}(s) G_C(s)} \quad (12)$$

$$q(s) = 1 + K_d \frac{L}{T_s} G_{PWM}(s) G_{LC}(s) - G_{PWM}(s) G_{LC}(s) G_C(s) = 0 \quad (13)$$

According to the stability criterion, the first column of Routh's array needs to be larger than 0 in order to guarantee the system stability. After mathematical calculation, the range of K_d can be obtained as:

$$0 < K_d < \frac{4}{3} + \frac{1}{6} \frac{T_s^2}{L_\alpha C_\alpha} \quad (14)$$

TS (Since the term $1/6 \cdot 2/L_\alpha C_\alpha$ is very small, it can be neglected for simplicity. Hence, the range of K_d can be obtained as:

$$0 < K_d < \frac{4}{3} \quad (15)$$

The deduced model of the deadbeat current control loop of the LC-HAPF is analyzed by using MATLAB and the system parameters including different K_d range is given in Table I.

As mentioned before, K_d should be selected as high as possible within the bounded value to minimize the steady-state error and shorten the response time. However, high K_d value will cause overshoot problem and lower the stability margin.

Table I

SYSTEM PARAMETERS FOR MATLAB SIMULATION	
System parameters	Physical values
L_α, C_α	8mH, 50μF
f_0 (fundamental frequency)	50 Hz
f_s (sampling frequency)	15 kHz
f_{sw} (switching frequency: deadbeat control)	10 kHz
K_d	0.2~1.2

To obtain a balance on steady-state error, overshoot and response time, K_d should be selected in around 0.8 to 1.1, which depends on desired performance. In this paper, $K_d = 0.8$ is chosen. The deduced model of the deadbeat current control loop of the LC-HAPF is analyzed by using MATLAB

and the system parameters including different Kd range is given in Table II. As mentioned before, Kd should be selected as high as possible within the bounded value to minimize the steady-state error and shorten the response time. However, high Kd value will cause overshoot problem and lower the stability margin. That means $ic_x \sim ic_x^*$, the compensating current can track its reference with less steady-state error, thus obtaining better current tracking performance. To obtain a balance on SteadyState error, overshoot and response time, Kd should be selected in around 0.8 to 1.1, which depends on desired performance.

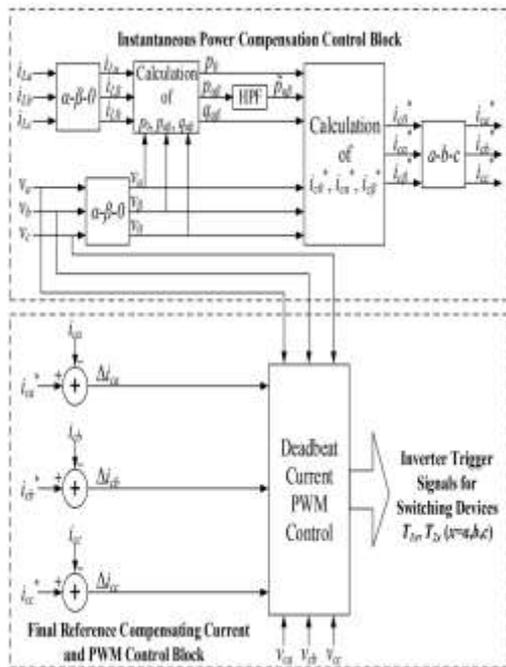


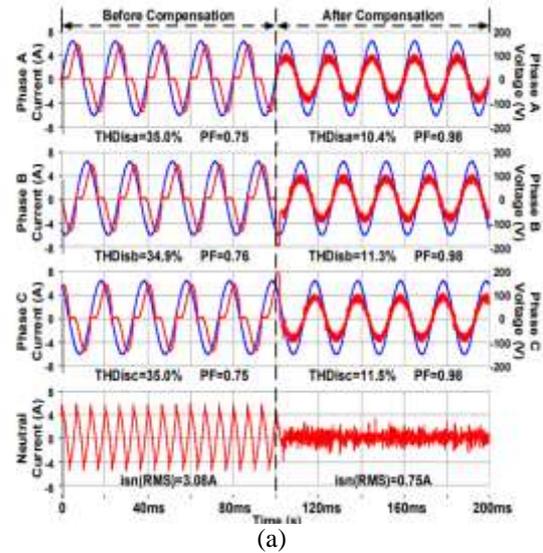
Fig. 8. The block diagram of proposed deadbeat current controller.

IV. SIMULATION RESULTS

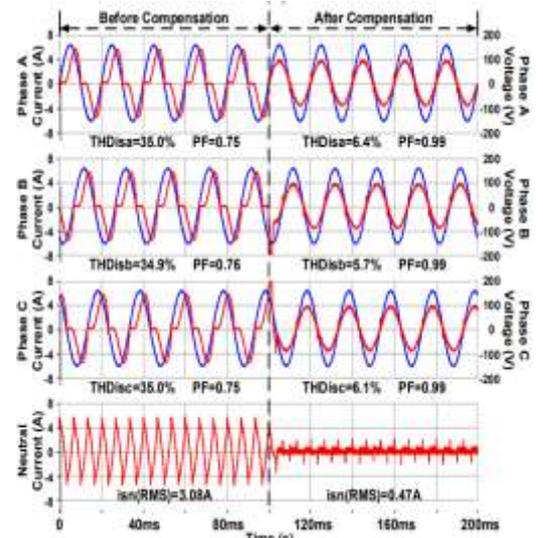
In the following, the simulation studies of the conventional hysteresis PWM controller, PI controller, MPR controller and deadbeat current controller for the three-phase four-wire center split LC-HAPF are carried out by using PSCAD/EMTDC. The corresponding simulation results before and after the hysteresis PWM controlled, the PI controlled, the MPR controlled and the deadbeat current controlled LC-HAPF compensation will be summarized in Fig. 9.

With reference to the IEEE standard 519-2014 [47], the acceptable Total Demand Distortion (TDD) = 15% with ISC/IL is in $100 < 1000$ scale (a small rating 110V-5kVA experimental prototype). The nominal rate current is assumed to be equal to the fundamental load current at the worst-case

analysis, which results in $THD = TDD = 15\%$. Therefore, this paper evaluates the LC-HAPF current harmonics compensating performance by setting an acceptable $THD = 15\%$.



(a)



(b)

Fig. 5.9 (a). Simulated results before and after LC-HAPF compensation with PI controller and (b) with proposed Dead-beat controller

The basic control principle of the hysteresis PWM control is based on deriving the switching signals from the comparison of the current error Δic_x between the reference compensating current ic_x^* and the actual compensating current ic_x with a fixed hysteresis band H. The trigger signals will drive the switching devices of the VSI in order to let ic_x tracks with its reference ic_x^* . Every time when the current error Δic_x is larger than the positive or smaller than the negative hysteresis band's boundary $ic_x^* + H$ or

icx* -H, a state change of the VSI's trigger signals occurs. The PI and PMR control is initially computing the current error signal icx by subtracting the reference compensating current icx^* by the actual compensating current icx . icx will be inputted into a PI / PMR controller. Then its corresponding output will be compared with a fixed frequency triangular carrier wave V_{tri} in order to generate the trigger signals for the switching devices of the VSI. Hysteresis PWM Controller Fig. 9(a) shows the simulation results of hysteresis PWM controller for the LC-HAPF. From Fig. 9(a), the system current ripples after compensation is obvious. From Fig. 9(a) and Table IV, although it can compensate the system displacement power factor (DPF) from 0.8 to unity, the system neutral current from 3.08 Arms to 0.75 Arms, the total current harmonics distortion (THD_{isx}) from 35% to about 11%, which satisfies the international standard of THD = 15% [47]. The system current ripples have been reduced significantly compared with the hysteresis PWM controller after compensation.

Deadbeat Current Controller Fig. 9(b) shows the simulation results of deadbeat current controller for the LC-HAPF. Compared with hysteresis PWM controller case, the system current ripples after compensation have been reduced significantly. From Fig. 9(b), it can compensate the system DPF from 0.8 to unity, the system neutral current from 3.08 Arms to 0.47 Arms, the THD_{isx} from 35% to less than 6.5%, which satisfies the international standard of THD = 15% [47]. It has the lowest percentage error of reactive power injection of less than 1%.

V. CONCLUSION

In this paper, an LCHAPF deadbeat current control approach is suggested, which may offer a cost-effective power quality compensation solution with minimal output current ripples and modest steady-state error. First, the suggested deadbeat current controlled LC-mathematical HAPF's modelling, and control block diagram are created and constructed. It is used to assess and debate the stability problem as well as parameter design considerations. Finally, the results of the deadbeat current controller for the LC-HAPF are shown in contrast to traditional hysteresis, PI, and PMR controllers, demonstrating its efficacy and improved compensatory capabilities.

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